# Advanced Soil Mechanics



BRAJA M. DAS



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Fourth Edition

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CRC Press Taylor & Francis Group 6000 Broken Sound Parkway NW, Suite 300 Boca Raton, FL 33487-2742

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International Standard Book Number-13: 978-1-4822-3483-1 (eBook - PDF)

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In the memory of my mother, and to Janice, Joe, Valerie, and Elizabeth

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