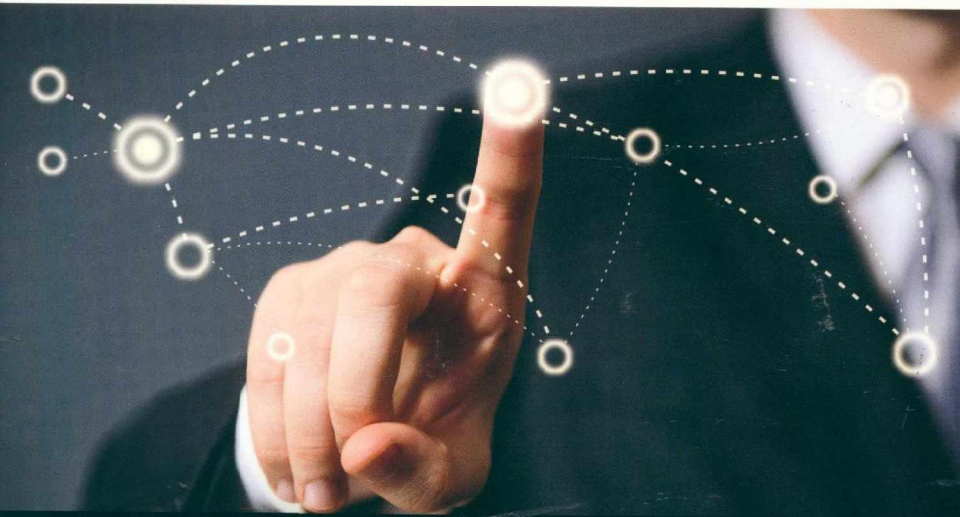
GLOBAL EDITION

Signals, Systems, and Transforms

FIFTH EDITION

Charles L. Phillips • John M. Parr • Eve A. Riskin



ALWAYS LEARNING

PEARSON

SIGNALS, SYSTEMS, AND TRANSFORMS

FIFTH EDITION

CHARLES L. PHILLIPS
Emeritus
Auburn University
Auburn, Alabama

JOHN M. PARR
University of Evansville
Evansville, Indiana

EVE A. RISKIN
University of Washington
Seattle, Washington

Global Edition contributions by

T. PRABHAKAR
GMR Institute of Technology,
Rajam, Andhra Pradesh

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PEARSON

To

Taylor, Justin, Jackson, Rebecca, and Alex

Michaela, Cadence, Miriam, and Connor Duncan,

Gary, Noah, and Aden

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